

1. **The Fundamental Theorem of Calculus, v1:** Let  $f$  be continuous on an open interval  $I$  containing  $a$ . Then

(a) the function  $A_f$  defined by

$$A_f(x) = \int_a^x f(t) \, dt$$

is defined for all  $x \in I$ ,

(b)  $\frac{d}{dx}(A_f(x)) = f(x)$ ,  
that is,  $A_f$  is an antiderivative of  $f$ .

2. **The Fundamental Theorem of Calculus, v2:** Let  $f$  be continuous on  $[a, b]$ , and let  $F$  be **any** antiderivative of  $f$ . Then

$$\int_a^b f(x) \, dx = F(b) - F(a)$$