

1. Find power series expansions about $x_0 = 0$ for the following .

(a) $f(x) = \sin(x)$

(b) $f(x) = \cos(x)$

Hint: $\frac{d}{dx} \sin(x) = \cos(x)$

(c) $\cos(x^2)$

Feel free to use the result from (b).

(d) $\int \cos(x^2) dx$

Then approximate $\int_0^1 \cos(x^2) dx$ accurate within 10^{-5} .

2. Find power series expansions of the following integrals.

If time, approximate the value of the following integrals accurate within 0.001.

(a) $\int_0^1 e^{-x^3} dx$

(b) $\int_0^{1/4} \frac{1}{1+x^4} dx$ Hint: $\frac{1}{1+x^4} = \frac{1}{1-(-x^4)}$