

## Recall – The Ratio Test:

Suppose that  $\sum_{k=1}^{\infty} a_k$  is a series of non-zero terms, and that

$$\lim_{k \rightarrow \infty} \left| \frac{a_{k+1}}{a_k} \right| = L.$$

Then

1. If  $L < 1$ , then  $\sum a_k$  converges absolutely.
2. If  $L > 1$  (or if  $L = \infty$ ), then  $\sum a_k$  diverges.
3. If  $L = 1$ , the Ratio Test is inconclusive.

2(c). Determine the convergence or divergence of  $\sum_{k=5}^{\infty} \frac{k^4 + 400k^3}{1000k^4 + k}$

3. Determine the absolute convergence, conditional convergence, or divergence of:

(a)  $\sum_{j=1}^{\infty} \frac{(-1)^j}{j + e^j}$

(b)  $\sum_{n=1}^{\infty} n \left(-\frac{2}{3}\right)^n$

(c)  $\sum_{m=2}^{\infty} \frac{(-1)^m m}{(m^2 - 1)^5}$

4. (All new!) Find all  $x$  for which the following series converge absolutely.

(a)  $\sum_{n=0}^{\infty} (-1)^n (2x)^n$

(b)  $\sum_{j=1}^{\infty} \frac{(-1)^j 2x^j}{j}$