

1. Let  $I = \int_0^1 x \sin(x^2) dx$

(a) Calculate  $L_4$  by hand.

Does this over-estimate or under-estimate  $I$ ?

(b) Write  $L_{10}$  and  $L_{50}$  using sigma notation.

(c) Use Maple to draw  $L_{10}$  and  $R_{10}$

(Use the `leftbox()` and `rightbox()` commands)

(d) Use Maple to calculate  $L_{10}$  and  $R_{10}$

(Use the `leftsum()` and `rightsum()` commands)

How does  $I$  compare to  $L_{10}$  and  $R_{10}$ ?

(e) Find the exact value of  $I$  by using  $u$ -substitution.

Does this make sense?

2. Approximate  $\int_0^{1.5} \cos(x^2) dx$  within .002 of its actual value.

**Hint:** Look at the graph of  $\cos(x^2)$ , and think about some of the ideas you had in the last problem.