

Determine whether each of the following improper integrals converges or diverges.

$$1. \int_2^\infty \frac{1}{x^3 + 2} dx$$

$$2. \int_5^\infty \frac{1}{\sqrt{x} - 2} dx$$

$$3. \int_2^\infty \frac{2}{\sqrt{x} + x^2} dx$$

$$4. \int_0^\infty \frac{2}{\sqrt{x} + x^2} dx$$