

Parametric equations for a surface in 3-space have the form

$$x = f(u, v) \quad y = g(u, v) \quad z = h(u, v).$$

There are two aspects to getting comfortable with parametric equations for surfaces:

1. Given the parametrization, understanding the surface.
2. Given the surface, being able to figure out the parametrization.

That is,

1. Given the parametric equations, what is the relationship between x , y , and z ?
2. Given the relationship between x , y , and z , what is the parametrization?

Recall:

$$\cosh(x) = \frac{e^x + e^{-x}}{2}$$

$$\sinh(x) = \frac{e^x - e^{-x}}{2}$$

Note: $\cosh(x)$ is always positive

Note: $\sinh(x)$ may be negative

In Class Work

- (a) Express the given surface using relationship(s) between x , y , and z .
- (b) Sketch traces & identify the surface without using Maple or the book.
- (c) Plot on Maple to check. Compare how Maple plots the parametric equations with how the surface looks using `implicitplot3d`.

1.

$$x = u \quad y = 3u^2 + 2v^2 \quad z = v.$$

2.

$$x = v \sinh(u) \quad y = 4v^2 \quad z = v \cosh(u).$$

Maple Example:

- ▶ `[2*cos(u)*sin(v), 2*sin(u)*sin(v), 6*cos(v)];`

right click on blue result

plots-plot builder - 3D parametric plot

- ▶ `(x/2)^2+(y/2)^2+(z/6)^2=1;`

right click on blue result

plots-3D implicit plot - x, y, z

Recall:

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- ▶ When we have $y = f(x)$, we parametrize that by $x = t, y = f(t)$.