Find the directions of maximum and minimum change of f at the given point, and the values of the maximum and minimum rates of change. 1. $f(x, y) = x^2 - y^3$, at the point (-1, -2)

$$abla f(x,y) = \langle 2x, -3y^2
angle \\
abla f(-1,-2) = \langle -2, -12
angle$$

The direction of maximum change of f at (-1, -2) is in the direction of the vector < -2, -12 >, and the value of this maximum increase is $\| < -2, -12 > \| = \sqrt{4 + 144} = \sqrt{148}$.

The direction of minimum change (that is the biggest decrease) is in the direction of < 2, 12 >, and the value of this greatest decrease is $-\sqrt{148}$.

Math 236-Multi (Sklensky)

Find the directions of maximum and minimum change of f at the given point, and the values of the maximum and minimum rates of change. 2. $f(x, y, z) = 4x^2yz^3$, at the point (1, 2, 1)

$$abla f(x, y, z) = \langle 8xyz^3, 4x^2z^3, 12x^2yz^2
angle
abla f(1, 2, 1) = \langle 16, 4, 24
angle$$

The direction of greatest increase (maximum change) is in the direction of < 16, 4, 24 >, with a value of $\sqrt{16^2 + 4^2 + 24^2} = \sqrt{848}$.

The direction of greatest decrease (minimum change) is in the direction of < -16, -4, -24 >, with a value of $-\sqrt{848}$.

Math 236-Multi (Sklensky)

Solutions to In-Class Work

March 31, 2010 2 / 2

▲□▶ ▲□▶ ▲ 臣▶ ▲ 臣▶ 臣 のへで