

Let  $G = U(20) = \{1, 3, 7, 9, 11, 13, 17, 19\}$  and  $H = \{1, 9\}$ .

1. Find all the left and right cosets of  $H$ .
2. For what values of  $a$  is  $aH = H$ ?
3. For what values of  $a$  is  $aH$  a subgroup of  $G$ ?
4. For what values of  $a$  and  $b$  is  $aH \cap bH \neq \emptyset$ ? In those cases, what is  $aH \cap bH$ ?

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