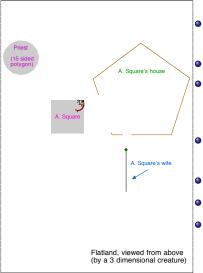
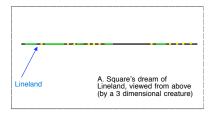
## Lower Dimensions



- In *Flatland*, Flatland exists not in 3 dimensions as our world does, but in 2.
- The world is a plane, not a space.
- Flatland residents can not see up or down, can not go over or under.
  - These concepts don't even exist!
- They *can* move left, right, forward, back, or at angles in plane
- Men are polygons, women are lines.
- Women are invisible from end-on.
- No matter what view he finds in Flatland, A. Square can never see the inside of the nearby Priest.

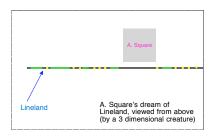
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- A. Square dreams he visits Lineland
  - A 1-dimensional world
  - No left or right, only forward and back
  - Men are line segments [green], women are points [yellow].

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## A. Square's Dream of Lineland

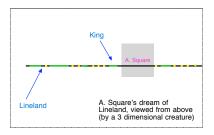


- A. Square tries to convince the King of Lineland of the existence of a 2nd dimension.
- One argument: A.Square can pass *through* Lineland.
- What would the King see and hear as A.Square passes through?
  - If A. Square passes through edge first (as illustrated)?
  - If A. Square passes through corner first?

• Edge first?

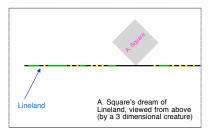
• Edge first?

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- Edge first?
- Corner first?

- Edge first?
- Corner first?



What else could A. Square do to try to convince the King of Lineland that he lives in a higher dimension?

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# How could a Sphere visiting Flatland convince A. Square of the existence of a third dimension?

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If we were visited by a 4-dimensional being, what would we see?
 Would there be any clues that it was a higher-dimensional being?

- If we were visited by a 4-dimensional being, what would we see?
  Would there be any clues that it was a higher-dimensional being?
- What (besides passing through our space) could it do to convince us that comes from a higher dimension?