Perspective Theorem

Set-up:



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Perspective Theorem

Set-up:

- Artist wants to represent object on canvas so that looking at canvas is like looking thru window at object.
- Canvas/window = picture plane. Lies between artist and object.
- Let the *xy*-plane= **picture plane**.
- Place origin so artist is located on negative z-axis.
- $d = \text{distance from artist's eye to origin. Artist's eye is at <math>(0, 0, -d)$.
- P(x, y, z) = any point on object. z > 0
- ▶ Let P' = image of P on picture plane= where line of sight from artist's eye to P crosses picture plane.
- P' on the picture plane= xy-plane ⇒ z-coordinate= 0. That is, P' has coordinates (x', y', 0).

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Perspective Theorem

Let the *xy*-plane represent the picture plane, and assume the artist's (or viewer's) eye is located at the point (0, 0, -d) (so that *d*, a positive number, is the distance from the artist's or viewer's eye to the picture plane.)

Given a point P(x, y, z) on an object, with z > 0 (that is, the object is beyond the picture plane), the coordinates x' and y' of its perspective image P'(x', y', 0) on the picture plane are given by

$$x' = \frac{dx}{d+z}$$
 $y' = \frac{dy}{d+z}$

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The Whole Room

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If we extend all lines representing lines in the actual classroom perpendicular (orthogonal) to the picture-plane, what happens?

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