

The curve formed by intersecting the plane y = 0 with the surface is a horizontal line

 $\frac{\partial f}{\partial x}$ will be zero at any point of the form (x, 0).



The curve formed by intersecting the plane x = 0 with the surface is also a horizontal line. $\frac{\partial f}{\partial y}$ will be zero at any point of the form (0, y)

March 29, 2010 1 / 4



The curve formed by intersecting the plane y = x with the surface is a much more interesting curve.

This means that the *directional derivatives* in this direction at points along this line will vary considerably.

Math 236-Multi (Sklensky)

In-Class Work

March 29, 2010 2 / 4

To find $\frac{\partial f}{\partial x}(a, b)$, we looked at

$$\frac{\partial f}{\partial x} = \lim_{h \to 0} \frac{f(a+h,b) - f(a,b)}{h}.$$

To find $\frac{\partial f}{\partial y}(a, b)$, we looked at

$$\frac{\partial f}{\partial y} = \lim_{h \to 0} \frac{f(a, b+h) - f(a, b)}{h}.$$

Math 236-Multi (Sklensky)

In-Class Work

March 29, 2010 3 / 4

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 三臣 - のへで

Find the following directional derivatives:

1.
$$f(x,y) = 2e^{4x/y} - 2x$$
, $(a,b) = (2,-1)$, in the direction of $< 1,3 >$

2.
$$f(x, y, z) = x^3yz^2 - 4xy$$
, $(a, b, c) = (1, -1, 2)$, in the direction of $< 2, 0, -1 >$.

(日) (四) (三) (三) (三)